

# Highlights of Fermat's Last Theorem

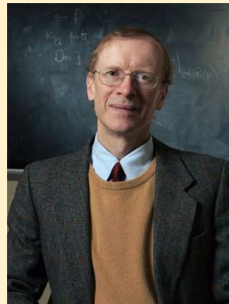
By: Bryce, Byron, and Martin (Team: A Definitely)

## Background:

- Pierre de Fermat was a 17th century French mathematician who discovered Fermat's Last Theorem and managed to prove cases  $n=4$ ,  $n=5$ , but did not finish the proof. [3]
- The first successful proof of Fermat's last Theorem was released in 1994 by Andrew Wiles. [1]
- Before Fermat's last theorem was proved by Sir. Wiles, many people have tried to prove it using very simple methods, and they all failed.



Pierre de Fermat



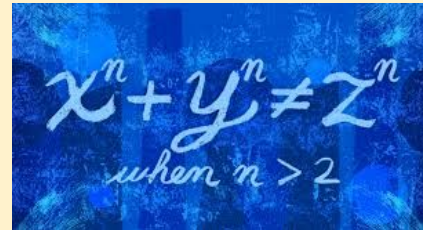
Andrew Wiles

## What is the theorem:

- Fermat's Last Theorem states that there are no natural numbers  $x$ ,  $y$ , and  $z$  such that  $X^n + y^n = z^n$ , where  $n$  is a natural number equal to 2 or more. [1]

## Applications:

- Fermat's last theorem can really be applied in number theory. [4]
- Gerhard Frey noticed that there was a connection between the equation  $X^n + y^n = z^n$  and the theory of elliptic curves. [1]
- Fermat's Last Theorem has contributed to high-speed computing. The theorem applies when  $l < 2000$  ( $l$  is the odd prime exponent in the Fermat relation). [6]



[7]

## Who is Andrew Wiles:

- Sir. Wiles was a mathematician who found Fermat's theorem to be quite fascinating.
- Sir. Wiles is a Royal Society Research Professor at the University of Oxford, specializing in number theory. [1]
- Sir. Wiles was the one who provided a proof for Fermat's theorem. With the aid from Richard Taylor, Wiles finished his proof that took him over six years to finish. [5]
- Once Wiles proof was accepted, he won the Abel prize. [5]

## Problems and How they were fixed:

- In 1993, Sir. Wiles presented his proof of the Taniyama-Shimura conjecture for semistable elliptic curves; together with Ribet's proof of the epsilon conjecture, but it was incorrect in the peer review, because it contained an error in a bound on the order of a particular group. It took him a year to fix the error, Sir. Wiles' proof succeeded by:
  - (1) Replacing elliptic curves with Galois representations,
  - (2) Reducing the problem to a class number formula,
  - (3) Tying up loose ends that arise because the formalisms fail in the simplest degenerate cases (Cipra 1995). [2]

## Further Research

- It would be interesting to know how Wiles combined all his theorems in his proof.
- What is the application field of Fermat's last theorem ?
- Has Mr. Wiles worked on solving any other theorems?

## Resources:

- [1][https://en.wikipedia.org/wiki/Fermat%27s\\_Last\\_Theorem](https://en.wikipedia.org/wiki/Fermat%27s_Last_Theorem)
- [2]<https://mathworld.wolfram.com/FermatsLastTheorem.html>
- [3]<https://www.quantamagazine.org/why-the-proof-of-fermats-last-theorem-doesnt-need-to-be-enhanced-20190603/>
- [4]<https://www.whitman.edu/Documents/Academics/Mathematics/byerleco.pdf>
- [5]<https://www.npr.org/sections/thetwo-way/2016/03/17/470786922/professor-who-solved-fermat-s-last-theorem-wins-math-s-abel-prize>
- [6]<https://www.ncbi.nlm.nih.gov/pmc/articles/PMC527932/pdf/pnas00728-0036.pdf>
- [7]<https://www.quantamagazine.org/why-the-proof-of-fermats-last-theorem-doesnt-need-to-be-enhanced-20190603/>